

| UČNI NAČRT PREDMETA / COURSE SYLLABUS | | | | | | |
|--|---------------------------|---|------------------------------|--|---|-------------|
| Predmet: | | Funkcionalna analiza | | | | |
| Course title: | | Functional analysis | | | | |
| Študijski program in stopnja Study programme and level | | Študijska smer Study field | | Letnik Academic year | Semester Semester | |
| Magistrski študijski program Matematika | | ni smeri | | 1 ali 2 | prvi ali drugi | |
| Master's study programme Mathematics | | none | | 1 or 2 | first or second | |
| Vrsta predmeta / Course type | | | | izbirni | | |
| Univerzitetna koda predmeta / University course code: | | | | M2116 | | |
| Predavanja Lectures | Seminar Seminar | Vaje Tutorial | Klinične vaje work | Druge oblike študija | Samost. delo Individ. work | ECTS |
| 45 | | 30 | | | 105 | 6 |
| Nosilec predmeta / Lecturer: | | prof. Peter Šemrl, prof. Roman Drnovšek | | | | |
| Jeziki / Languages: | | Predavanja / Lectures: slovenski/Slovene, angleški/English | | | | |
| | | Vaje / Tutorial: slovenski/Slovene, angleški/English | | | | |
| Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti: | | | | Prerequisites: | | |
| | | | | | | |
| Vsebina: | | | | Content (Syllabus outline): | | |
| Banachovi prostori. Linearni operatorji in funkcionali na Banachovih prostorih. Izrek o odprti preslikavi. Izrek o zaprtem grafu. | | | | Banach spaces. Linear operators and functionals on Banach spaces. The open mapping theorem. The closed graph theorem. The principle of uniform boundedness. The second dual. The | | |

| | |
|--|--|
| <p>Princip enakomerne omejenosti. Drugi dual.</p> <p>Adjungirani operator na Banachovem prostoru.</p> <p>Šibke topologije. Banach-Alaoglujev izrek.</p> <p>Krein-Milmanov izrek o ekstremnih točkah.</p> <p>Banachove algebre. Ideali in kvocienti. Spekter elementa. Rieszov funkcijski račun. Gelfandova transformacija.</p> <p>C^*-algebre. Približne enote. Ideali in kvocienti. Komutativne C^*-algebre. Funkcijski račun v C^*-algebrah. Gelfand-Naimark-Segalova konstrukcija.</p> | <p>adjoint operator on a Banach space . Weak topologies. The Banach-Alaoglu theorem. The Krein-Milman theorem on extreme points. Banach algebras. Ideals and quotients. The spectrum of an element. Riesz functional calculus. The Gelfand transform. C^*-algebras. Approximate units. Ideals and quotients. Commutative C^*-algebras. The functional calculus in C^*-algebras. The Gelfand-Naimark-Segal construction.</p> |
|--|--|

Temeljni literatura in viri / Readings:

B. Bollobás: Linear Analysis : An Introductory Course, 2nd edition, Cambridge Univ. Press, Cambridge, 1999.

J. B. Conway: A Course in Functional Analysis, 2nd edition, Springer, New York, 1990.

Y. Eidelman, V. Milman, A. Tsolomitis: Functional Analysis : An Introduction, AMS, Providence, 2004.

M. Hladnik: Naloge in primeri iz funkcionalne analize in teorije mere, DMFA-založništvo, Ljubljana, 1985.

R. Meise, D. Vogt: Introduction to Functional Analysis, Oxford Univ. Press, Oxford, 1997.

G. K. Pedersen: Analysis Now, Springer, New York, 1996.

W. Rudin: Functional Analysis, 2nd edition, McGraw-Hill, New York, 1991.

I. Vidav: Linearni operatorji v Banachovih prostorih, DMFA-založništvo, Ljubljana, 1982.

- I. Vidav: Banachove algebre, DMFA-založništvo, Ljubljana, 1982.

I. Vidav: Uvod v teorijo C^* -algeber, DMFA-založništvo, Ljubljana, 1982.

Cilji in kompetence:

Objectives and competences:

Slušatelj spozna osnove funkcionalne analize in povezavo z drugimi področji analize.

Students learn the basics of functional analysis and links with other areas of analysis.

Predvideni študijski rezultati:

Znanje in razumevanje: Obvladanje osnovnih pojmov funkcionalne analize. Sposobnost rekonstrukcije (vsaj lažjih) dokazov.
Sposobnost aplikacije pridobljenega znanja.
Uporaba: Uporaba funkcionalne analize sega tudi v naravoslovje in druga področja znanosti kot na primer ekonomijo.

Refleksija: Razumevanje teorije na podlagi uporabe.

Prenosljive spretnosti – niso vezane le na en predmet: Sposobnost abstraktnega razmišljanja. Spretnost uporabe domače in tuje literature.

Intended learning outcomes:

Knowledge and understanding: Understanding basic concepts of functional analysis. Ability of the reconstruction (at least easier) proofs.
Ability of the application of acquired knowledge.

Application: Functional analysis is used in natural sciences and other areas of science such as economics.

Reflection: Understanding of the theory on the basis of examples.

Transferable skills: Ability to use abstract methods to solve problems. Ability to use a wide range of references and critical thinking.

Metode poučevanja in učenja:

predavanja, vaje, domače naloge, konzultacije

Learning and teaching methods:

Lectures, exercises, homeworks, consultations

Načini ocenjevanja:

Delež (v %) /

Weight (in %)

Assessment:

Način (pisni izpit, ustno izpraševanje, naloge, projekt):
domače naloge

10%
50%
40%

Type (examination, oral, coursework, project):
homeworks

| | | |
|---|--|---|
| izpit iz vaj | | written exam |
| ustni izpit | | oral exam |
| Ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL) | | Grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL) |

Reference nosilca / Lecturer's references:

Roman Drnovšek:

- DRNOVŠEK, Roman. Common invariant subspaces for collections of operators. Integral equations and operator theory, ISSN 0378-620X, 2001, vol. 39, no. 3, str. 253-266 [COBISS.SI-ID 10597721]
- DRNOVŠEK, Roman. Invariant subspaces for operator semigroups with commutators of rank at most one. Journal of functional analysis, ISSN 0022-1236, 2009, vol. 256, iss. 12, str. 4187-4196 [COBISS.SI-ID 15167321]
- DRNOVŠEK, Roman. An infinite-dimensional generalization of Zenger's lemma. Journal of mathematical analysis and applications, ISSN 0022-247X. [Print ed.], 2012, vol. 388, iss. 2, str. 1233-1238 [COBISS.SI-ID 16214617]

Peter Šemrl:

- ŠEMRL, Peter. Applying projective geometry to transformations on rank one idempotents. Journal of functional analysis, ISSN 0022-1236, 2004, vol. 210, no. , str. 248-257 [COBISS.SI-ID 13012825]
- ŠEMRL, Peter. Similarity preserving linear maps. Journal of operator theory, ISSN 0379-4024, 2008, vol. 60, no. 1, str. 71-83 [COBISS.SI-ID 15079257]
- ŠEMRL, Peter. Symmetries on bounded observables: a unified approach based on adjacency preserving maps. Integral equations and operator theory, ISSN 0378-620X, 2012, vol. 72, iss. 1, str. 7-66 [COBISS.SI-ID 16568665]